

MAR650 Homework Problem 1:

Use the parameters listed in Table 1, light functions listed in Table 2 and nutrient uptake functions and temperature relationship introduced in the lecture to calculate the gross growth rate of phytoplankton at the sea surface and a depth of 50 m at two selected stations on Georges Bank and in the Gulf of Maine. Summarize your finding as a short report.

Locations: Two stations: a) station O, located in the Gulf of Maine and b) station C, located over Georges Bank.

Table 1: Biological and physical parameters:

Definition	Station O	Station C
Solar irradiance at the sea surface	300 W/m ²	300 W/m ²
Light attenuation coefficient k	0.05 m ⁻¹	0.1 m ⁻¹
Water temperature at the sea surface	18°C	14°C
Water temperature at 50 m	8°C	14°C
Nitrate at the sea surface	0.4 μmol/L	1.0 μmol l ⁻¹
Nitrate at 50 m	2.0 μmol/L	1.0 μmol/L
Silicate at the sea surface	0.8 μmol/L	2.0 μmol/L
Silicate at 50 m	4.0 μmol/L	2.0 μmol/L
Phosphorus at the sea surface	0.03 μmol/L	0.2 μmol/L
Phosphorus at 50 m	0.4 μmol/L	0.2 μmol/L
Maximum growth rate μ_{max}	2 d ⁻¹	2 d ⁻¹
Optimal water temperature T_o	20°C	20°C
Nitrate half-saturation constant K_{NO_3}	1.0 μmol/L	1.0 μmol/L
Silicate half-saturation constant K_{Si}	1.5 μmol/L	1.5 μmol/L
Phosphorus half-saturation constant K_{PO_4}	0.1 μmol/L	0.1 μmol/L
Temperature coefficient a	0.07	0.07

Table 2: Functions of $f(I)$ included in the FVCOM Biological Module

Function Name	Equation	Parameter value
(1) SL62_LIGHT	$\frac{I}{I_{opt}} e^{\left(1 - \frac{I}{I_{opt}}\right)}$	$I_{opt}=100$ (Wm ⁻²)
(2) MM_LIGHT	$\frac{\alpha_I I}{K_I + \alpha_I I}$	$\alpha_I=1; K_I=50$ (Wm ⁻²)
(3) LB_LIGHT	$\frac{\alpha_I I}{\sqrt[n]{K_I^n + (\alpha_I I)^n}}$	$\alpha_I=1; K_I=50$ (Wm ⁻²); n=2

(4) V65_LIGHT	$\frac{\alpha_I I}{\sqrt{I_{opt}^2 + \alpha_I^2 I^2}} \frac{1}{[1 + (\beta \frac{I}{I_{opt}})^2]^{n/2}}$	$\alpha_I=1; I_{opt}=100(\text{Wm}^{-2});$ $n=1; \beta=1.$
(5) PE78_LIGHT	$\frac{I}{I_{opt}} \frac{2 + \alpha_I}{1 + \alpha_I \frac{I}{I_{opt}} + \left(\frac{I}{I_{opt}}\right)^2}$	$\alpha_I=1; I_{opt}=100(\text{Wm}^{-2})$
(6) WNS74_LIGHT	$1 - e^{-\frac{\alpha_I I}{\mu_{max}}}$	$\alpha_I=0.01$
(7) PGH80_LIGHT	$(1 - e^{-\frac{\alpha_I I}{\mu_{max}}}) e^{-\frac{\beta I}{\mu_{max}}}$	$\alpha_I=0.01; \beta=0.0001$
(8) JP76_LIGHT	$\tanh\left(\frac{\alpha_I I}{\mu_{max}}\right)$	$\alpha_I=0.01;$
(9) BWDC99_LIGHT	$\frac{\tanh\left[\frac{\alpha_I (I - I_o)}{\mu_{max}}\right] e^{\beta(I_{opt} - I)}}{\mu_{max}}$	$\alpha_I=0.01; \beta=0.0001; I_o=1$ $(\text{Wm}^{-2}); I_{opt}=100 (\text{Wm}^{-2})$